

Introduction

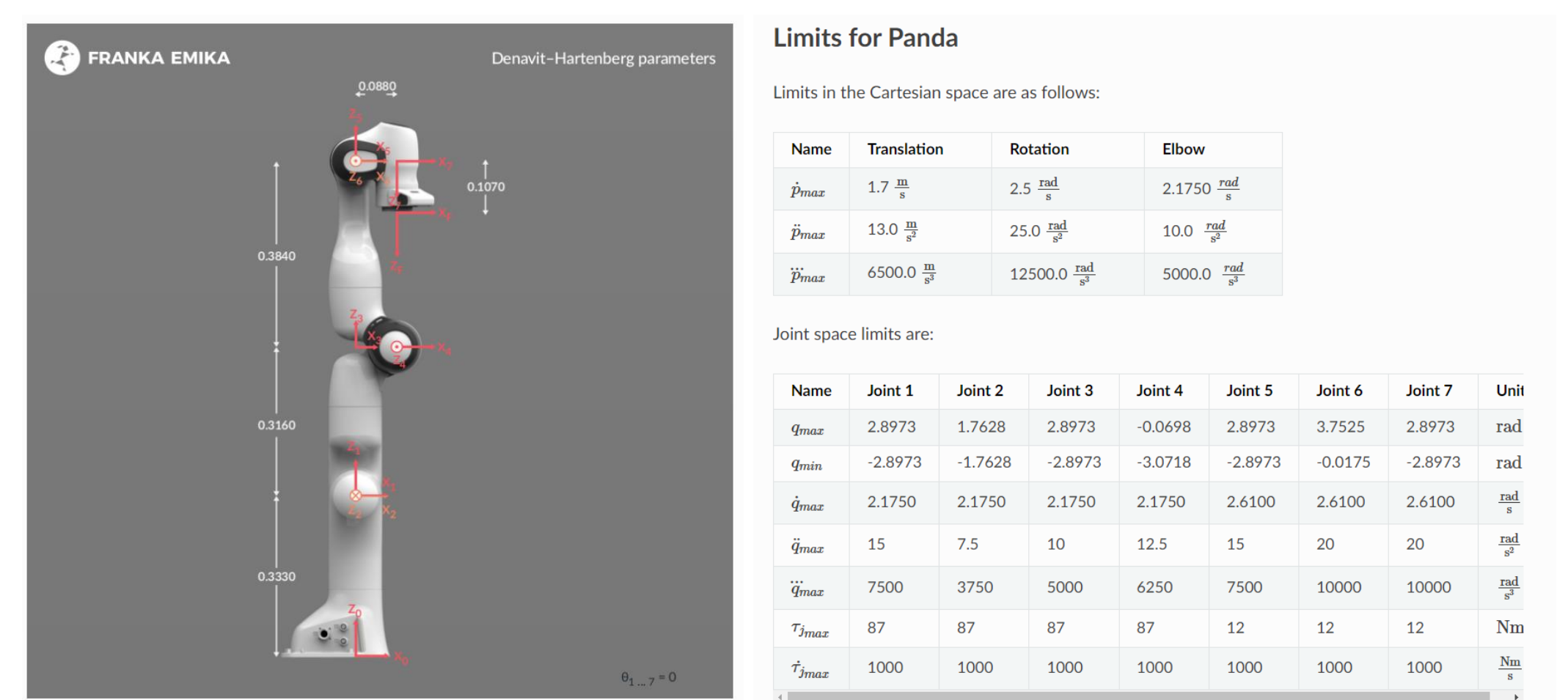
Human can throw different objects in various ways, adaptive to unstructured environments. Can we design reliable and efficient algorithms for robots to do so?



Challenges

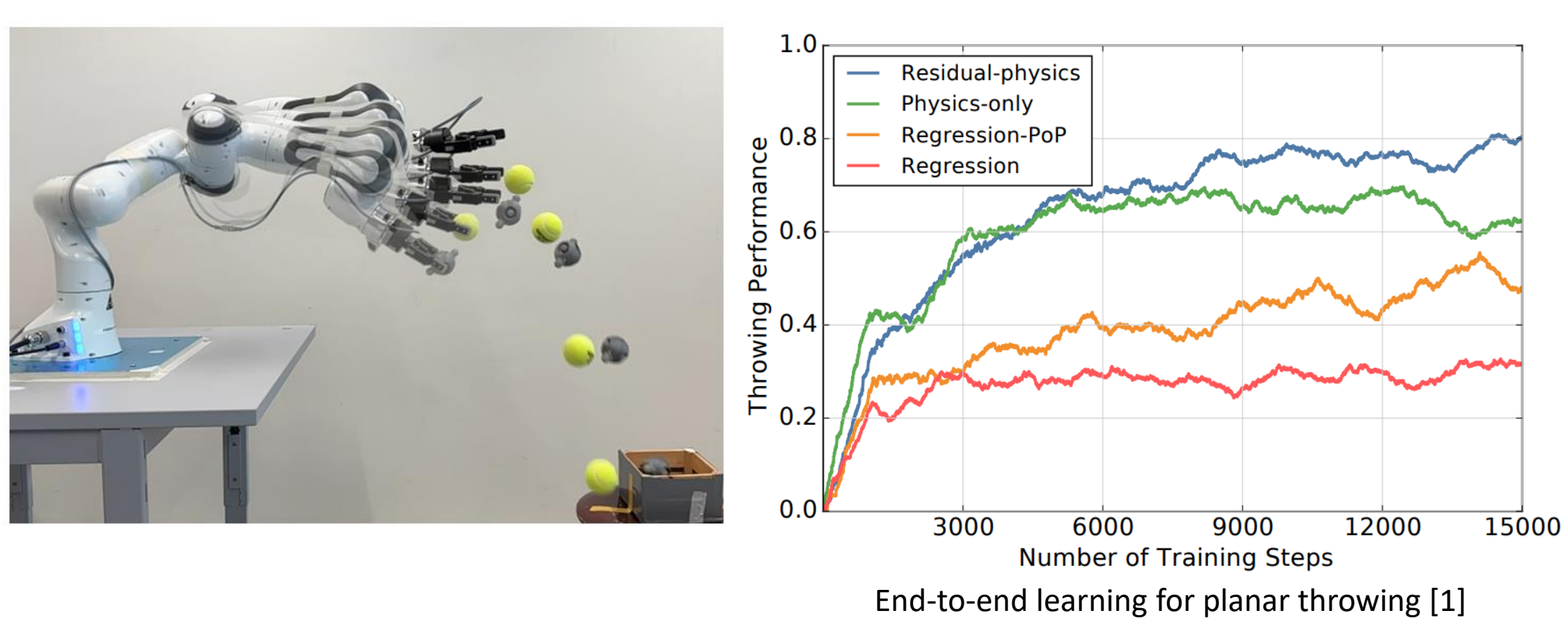
Dexterous throwing - nonconvex feasible set

- Complex geometry of the 7-DoF robot
- Restrictive dynamic limits

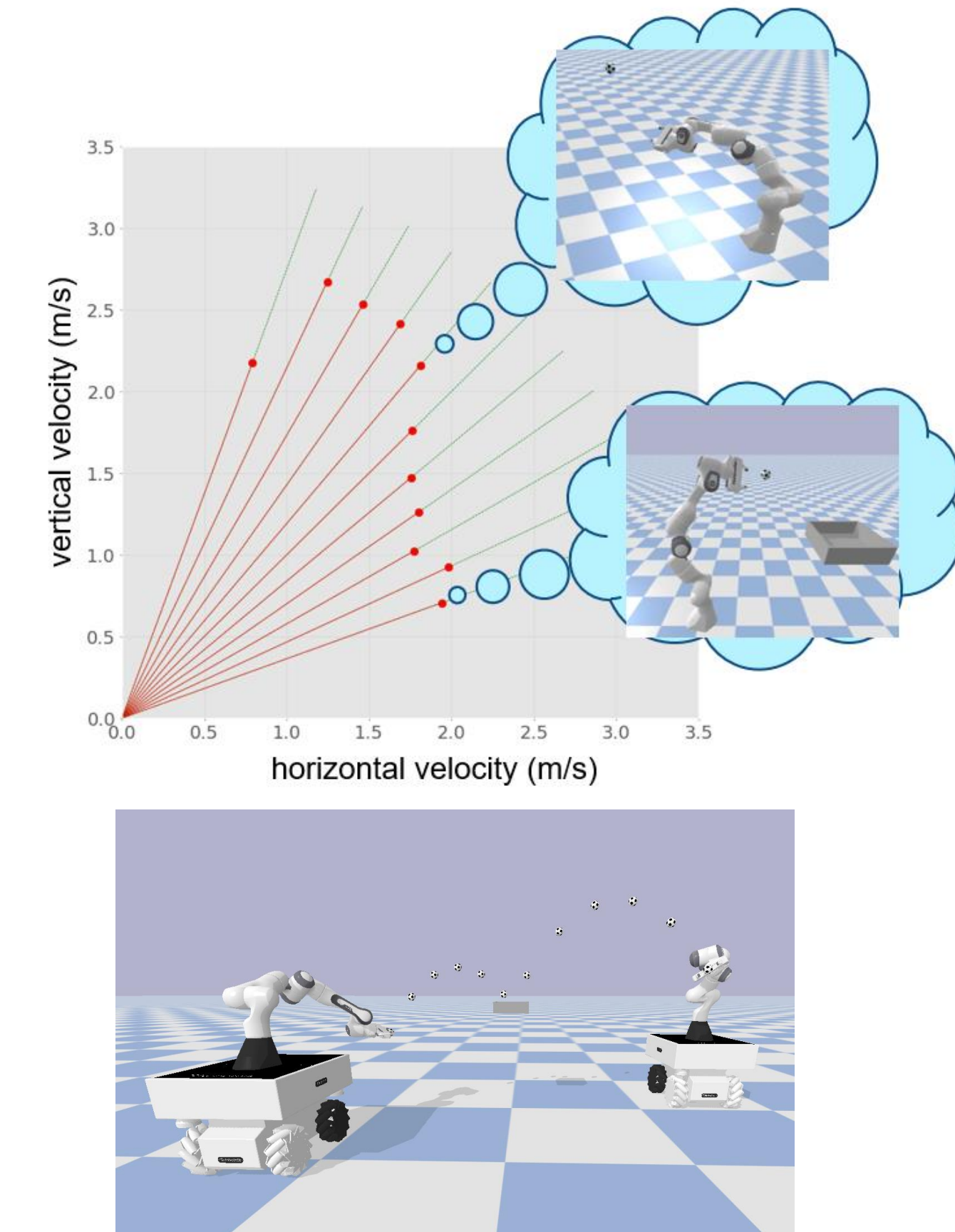


Release uncertainty – intricate contact mechanics

- Objects differ in friction and deformation
- Same throwing motion could lead to different landing outcomes
- End-to-end learning is not scalable to diverse configurations



Velocity Hedgehog – Dictionary of Diverse Throwing Configurations [2]



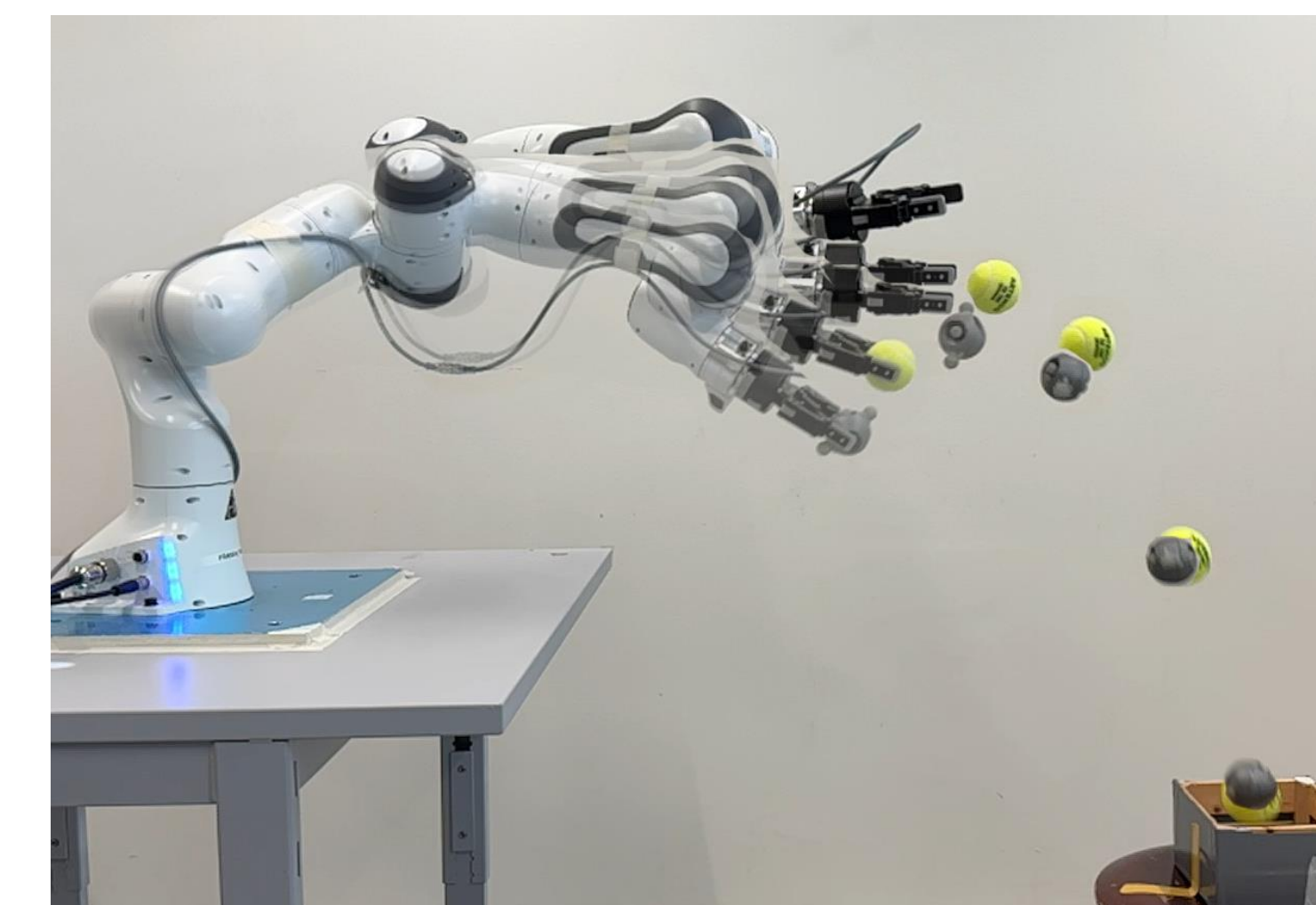
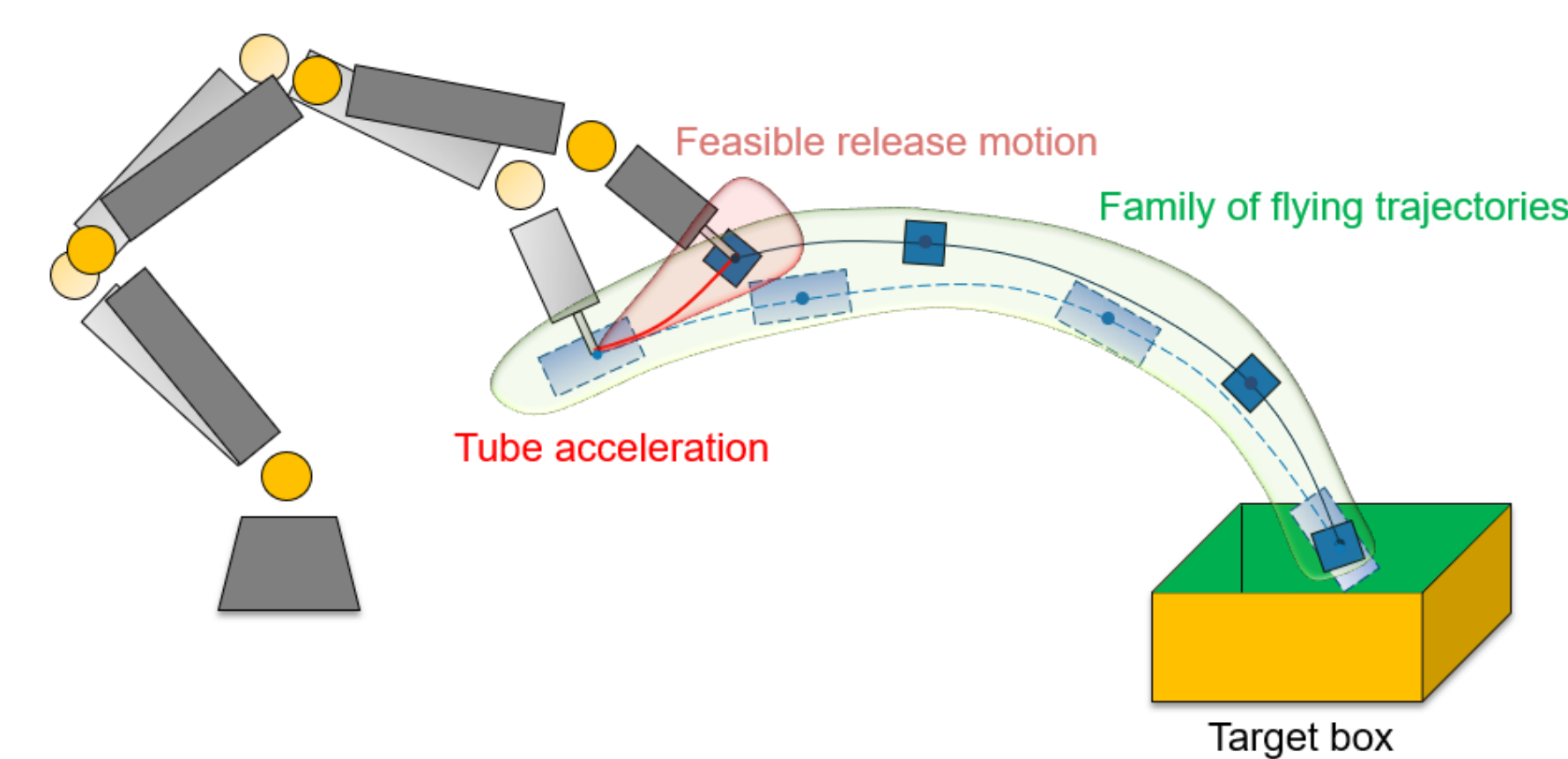
Offline: build throwing dictionary

- Keys: 100k pairs of (end-effector position, throwing direction)
- Value of each key:
 - maximum feasible Cartesian velocity v_{max}
 - the joint configuration enabling v_{max}
- Extracted from 1 million joint configurations (7 hours)

Online: search over 100k entries

- 20 ms running time
- Thousands of qualitatively different solutions

Tube Acceleration - Robust Release Motion

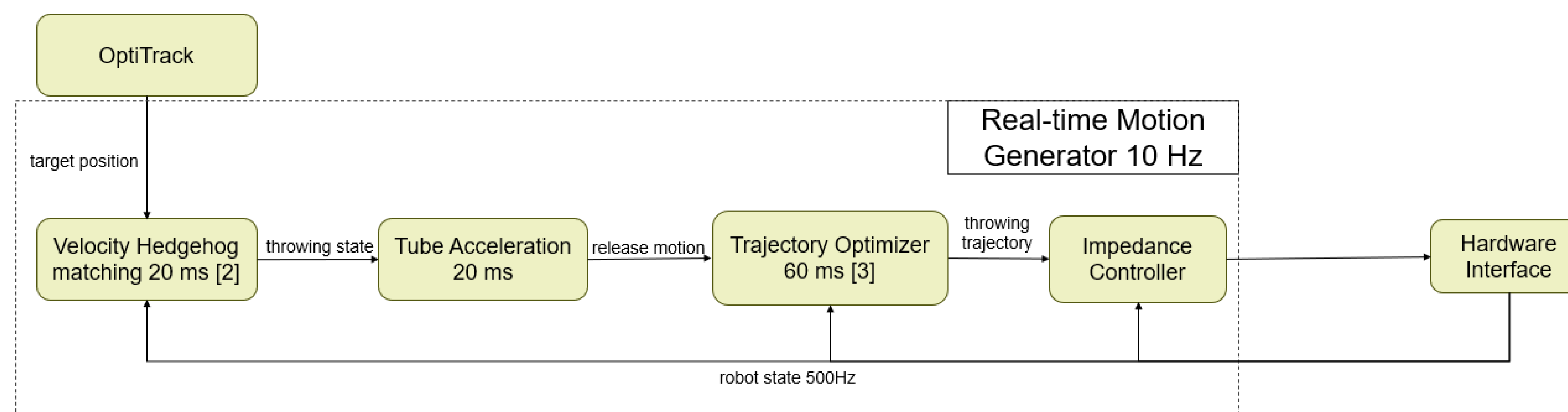


Idea: design robot motion to traverse the family of valid throwing configurations during gripper opening (100 ms)

Insight: object flying flowmap: initial state → landing position is quasi-linear (bounded Hessian)

- Constant joint acceleration – tube acceleration during release window can drive the robot stay in valid throwing configurations
- Tube acceleration can be found via convex optimization within 20 ms and with bounded error

System Architecture

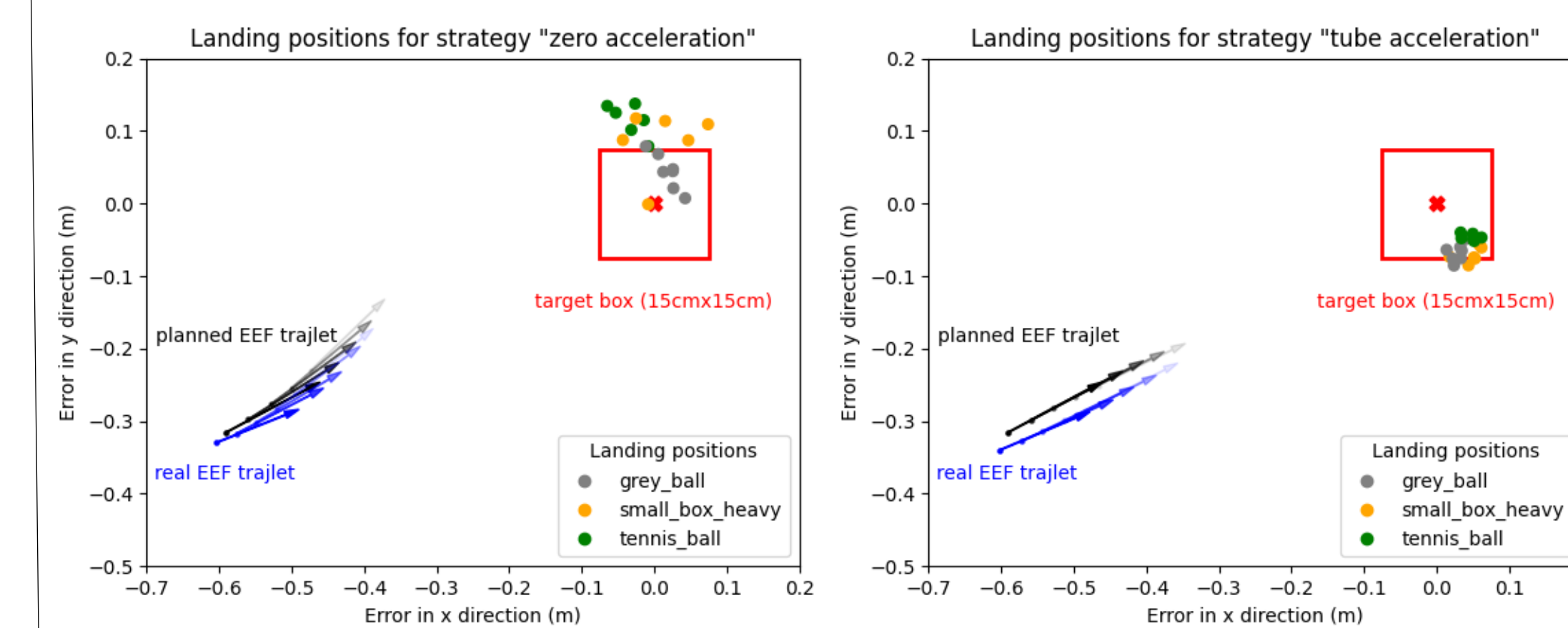


Real Throwing Experiments

Thrown objects

Object	grey_ball	small_box_heavy	tennis_ball
Weight (g)	120	100	70
Size (mm)	80×60×60	80×65×60	75×75×75

Population of landing positions



Statistics of landing errors

Object	Mean (mm)		Std. (mm)	
	Tube	Zero	Tube	Zero
grey_ball	74.52	53.70	9.51	15.60
small_box_heavy	87.12	95.30	7.47	44.57
tennis_ball	66.23	121.07	9.55	25.97
overall	75.88	88.11	12.04	40.74

Conclusion

- Dexterous throwing configurations can be found quickly via Velocity Hedgehog
- Release uncertainty can be suppressed by robust throwing motion design
- Fast and reliable algorithms enable adaptive robot throwing

Reference

[1] Zeng et al., "TossingBot: Learning to Throw Arbitrary Objects with Residual Physics", RSS 2019.

[2] Yang Liu, Aradhana Nayak and Aude Billard, "A Solution to Adaptive Mobile Manipulator Throwing", IROS 2022.

[3] Petr Listov and Colin Jones, "PolyMPC: An efficient and extensible tool for real-time nonlinear model predictive tracking and path following for fast mechatronic systems", Optimal Control Applications and Methods 2020.

Acknowledgement: The authors acknowledge the H2020 ICT-46-2020 EU project DARKO for supporting this work.